Critical degrees of saturation at freezing of porous and brittle materials

Fagerlund, Göran

1973

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CRITICAL DEGREES OF SATURATION AT FREEZING OF POROUS AND BRITTLE MATERIALS

GÖRAN FAGERLUND

LUND 1973
Rättelselista till
"CRITICAL DEGREES OF SATURATION AT FREEZING OF POROUS AND BRITTLE
MATERIALS" av Göran Fagerlund

I listan tas endast med sådana fel, som kan leda till missförstånd
av innehållet.

\[ u = \text{uppfirån} \quad n = \text{nerifrån} \]

**DEGRI CRITIQUE DE SATURATION ..........etc ...........

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<tr>
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<th>Står</th>
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<td>271</td>
<td>Notations</td>
<td>D&lt;sub&gt;CR&lt;/sub&gt;</td>
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<td>272</td>
<td>&quot;</td>
<td>( t_0 )</td>
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<td>275</td>
<td>&quot;</td>
<td>k</td>
<td>k</td>
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<td>284</td>
<td>Summary</td>
<td>ekv (10)</td>
<td>K</td>
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**KRITISKA VATTENMÅTTNADSGRADER .......... (Rapport 34)

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<tr>
<td>32</td>
<td>översta ekv</td>
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<tr>
<td>40</td>
<td>17 n</td>
<td>0,99</td>
<td>0,92</td>
</tr>
<tr>
<td>42</td>
<td>ekv (45)</td>
<td>a</td>
<td>( \ell )</td>
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<tr>
<td>62</td>
<td>ekv (68)</td>
<td>( 10^2 )</td>
<td>( 10^{-2} )</td>
</tr>
<tr>
<td>65</td>
<td>ekv (76) o (77)</td>
<td></td>
<td>multipliceras med ( \Delta \ell )</td>
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<tr>
<td>69</td>
<td>ekv (83)</td>
<td>28,5</td>
<td>19,6</td>
</tr>
<tr>
<td>73</td>
<td>ekv (91)</td>
<td>0,0085 ( \theta )</td>
<td>-0,0085 ( \theta )</td>
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<tr>
<td>80</td>
<td>16 u</td>
<td>0,192</td>
<td>( \frac{192}{192} )</td>
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<tr>
<td>80</td>
<td>ekv (102)</td>
<td>+0,25 ( \Delta W_n )</td>
<td>-0,75 ( \Delta W_n )</td>
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<tr>
<td>94</td>
<td>18 u</td>
<td>Där ( k_1 ) är</td>
<td>Där ( k_2 ) är</td>
</tr>
<tr>
<td>97</td>
<td>17 n</td>
<td>2/1000</td>
<td>2/1000 mm</td>
</tr>
<tr>
<td>130</td>
<td>16 n</td>
<td>30x30 cm(^2)</td>
<td>30x30 mm(^2)</td>
</tr>
<tr>
<td>130</td>
<td>ekv (129)</td>
<td>TOT</td>
<td>( x_{\text{TOT}} )</td>
</tr>
<tr>
<td>156</td>
<td>ekv (140)</td>
<td>k ( \cdot \log t )</td>
<td>-k ( \cdot \log t )</td>
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<tr>
<td>249</td>
<td>fig 48</td>
<td>K = ( \frac{W_e}{\ell P} )</td>
<td>K = ( \frac{W_e}{\ell P} )</td>
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**SIGNIFICANCE OF CRITICAL DEGREES ..........etc ...........

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<th>Sid</th>
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<tr>
<td>12</td>
<td>18 u</td>
<td>&quot;slow air&quot;</td>
<td>&quot;slow water&quot;</td>
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<tr>
<td>18</td>
<td>ekv (21)</td>
<td>( \sqrt{P(1-K)} )</td>
<td>P(1-K)</td>
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<tr>
<td>21</td>
<td>ekv (25)</td>
<td>1000 ( \ell_0/C )</td>
<td>1000 ( \ell_0/C )</td>
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<tr>
<td>22</td>
<td>under ekv (32)</td>
<td>curved</td>
<td>cured</td>
</tr>
<tr>
<td>22</td>
<td>ekv (33)</td>
<td>28,5</td>
<td>19,6</td>
</tr>
</tbody>
</table>
** forts SIGNIFICANCE OF CRITICAL DEGREES ... etc ... **

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<thead>
<tr>
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<tbody>
<tr>
<td>22</td>
<td>ekv (33)</td>
<td>$\ln\left(\frac{To-T}{To}\right)$</td>
<td>$\ln\left(\frac{To-\Delta T}{To}\right)$</td>
</tr>
<tr>
<td>23</td>
<td>ekv (34)</td>
<td>(To-T)</td>
<td>(To-ΔT)</td>
</tr>
</tbody>
</table>

**METHODS OF CHARACTERIZATION ... etc ...**

**Avsnittet "suction porosimetry"**

| 17  | ekv (34) | $\sum B_i$ | $\sum (B_i - B_{i-1})$ |
| 20  | ekv (40) | $\sum B_i$ | $\sum (B_{i+1} - B_i)$ |

**Avsnittet "freezing point depression"**

| 5   | ekv (11) | $(1+1,84 \cdot 10^{-3})$ | $(1+1,84 \cdot 10^{-3} \Delta T)$ |
|     |          | $-0,40 \cdot 10^{-6}$   | $-0,40 \cdot 10^{-6} \Delta T^2$ |
| 6   | ekv (16) | $- \frac{\Delta T}{To} = \ln \frac{To}{To-\Delta T}$ | $\frac{\Delta T}{To} = \ln \frac{To}{To-\Delta T}$ |
| 10  | ekv (29) | 5                      | 1,63 |
| 10  | ekv (30) | 28,5                   | 19,6 |

**Avsnittet "BET-method"**

| 8   | 10 n     | $10^{-4}$          | $10^2$ |
| 8   | 9 n      | $10^{-5}$          | $10^{-7}$ |

GF/ABW 10.5.73
This thesis comprises the following reports under the general heading "Critical Degrees of Saturation at Freezing of Porous and Brittle Materials":


INTRODUCTION

This thesis is based on experimental work carried out during the period 1968-1972. The whole investigation is sponsored by the Swedish Council for Building Research and has been performed at the department of Building Materials at the Lund Institute of Technology.

The thesis treats the problem frost resistance of building materials, a problem which is far from being solved despite much scientific work in many countries. According to the author the main reason for this lack of success is, that the problem of frost resistance is not only a function of materials properties but also of properties of the environment in which the materials are used. Hence, in order to solve the problem it is necessary to investigate separately the effect of material properties and the effect of environmental properties on the frost resistance of a material.

This distinction between influence of material and influence of environment may seem very logical or even to be a truism. However, very few scientists have made such an approach to the problem. Instead the research has principally been aimed at finding correlations between laboratory freezing-tests and behaviour of the material of practice. The debate among the scientists has to a big extent consisted in how to choose freezing method for a certain material in a certain situation in order to get the best correlation. Thus, in the normal way of treating the problem frost resistance, material and environment are "mixed together" in a way which obscures the solution of the problem.

In the work presented here a distinction between material and environment is made. Materials properties as well as properties of environment are expressed in terms of "degree of saturation" defined:

\[ S_f = \frac{w_f}{w_f + z} \]

where \( S_f \) is effective degree of saturation, \( w_f \) is the maximum freezable water content at the lowest temperature used and \( z \) is the air-filled pore-volume before freezing.

The materials properties are expressed in a "critical degree of saturation", \( S_{CR} \), which corresponds to the maximum water content which can be held in a specimen without risk of frost damage at a freezing.

The properties of environment are expressed in "actual degrees of saturation", \( S_{ACT} \), which corresponds to the water contents a certain material will reach in a certain environment.

\( S_{CR} \) is supposed to be a materials constant. Its value may of course pass through a certain change with time since a material may be used for many decades, why the relevant materials properties may change.

\( S_{ACT} \) varies with time since the wetness of the environment is a variable with time.

Of course the separation of materials and environmental properties are not complete. Above all the hydraulic properties of the material is fundamental for the value of \( S_{CR} \). However for an estimation of the frost resistance of a certain material used in different environments the separation is logical and helps to clarify the complex problem of frost resistance.

The aim of the thesis is to theoretically and empirically prove the existence of critical degrees of saturation, to advise a new rational method of freeze-testing materials and above all to discuss the significance and serviceableness of the critical degrees of saturation. The last part also includes theoretical and experimental studies of
mechanisms of destruction by frost, of freezing characteristics of pore water and of connections between materials properties and frost resistance

DEFINITION OF FROST RESISTANCE (Reports 1 and 2)
The frost resistance, \( F \), is defined;
\[
F = S_{CR} - S_{ACT}
\]  
(2)
If \( S_{CR} \) is considered constant the frost resistance will vary with time according to the way \( S_{ACT} \) varies with time. Frost damage will occur when \( F < 0 \) at subfreezing temperatures.
Hence the problem of frost resistance is of a statistical nature since the occurrence of the dangerous combination subfreezing temperature and too high water content depends on statistical factors such as frequency of freezing point passages, of wetness of the environment etc.

CHOICE OF MATERIALS AS REGARDS FROST RESISTANCE (Reports 1 and 2)
According to eq (2) the frost resistance of an arbitrary material can be quantified. This makes rational choices of material as regards frost resistance possible.
The way of choosing material can be directly compared to a normal choice or design of a structural component as regards strength /1/.

FREEZE-TEST METHOD (Report 2)
A freeze test method will be divided in two parts of quite different character:
- **Part 1**: Determination of critical degrees of saturation. The same type of method is used for each material.
- **Part 2**: Determination of actual degrees of saturation. The method should from a theoretical point of view be designed according to the actual way of using the material.
Part 1 is principally dependent only on materials properties and part 2, for each material, principally dependent only on properties of the environment.
In /2/ are given comprehensive descriptions and discussion of methods of determination of \( S_{CR} \). This can be done by multi-cycle experiments followed by measurements of damage after terminated freezing cycles or by one-cycle experiments accompanied by simultaneous measurements of for instance length change of the specimen.
Critical degrees of saturation have been measured for 41 different porous materials, normally by multi-cycle experiments. The results are shown and discussed in /2/.
\( S_{ACT} \) can from a theoretical point of view only be determined by experiments exactly reproducing the actual environment which demands knowledge of climate-data and of moisture measurement methods. Another way of solving this part of the frost resistance problem is to use moisture mechanics in an analytical calculation. Both those methods are however inapplicable for the present day since almost all information needed is lacking.
As a substitute simple water absorption tests can be used. Comparisons found in literature /2/ between water contents of different materials in practice and water absorption of the same materials in laboratory have shown, that the in-situ-values often corresponds to many days of capillary water absorption. Hence each material ought to get a lower value of $S_{\text{ACT}}$ at many days water uptake then its $S_{\text{CR}}$ if the material is to be frost resistant.

In /2/ is shown in which way a water absorption test can be performed. It is also discussed the influence on frost resistance of rate of water absorption, of rate of drying, of the so called critical thickness and of specimen size.

Practical experiments have been performed with all the materials for which $S_{\text{CR}}$ have been determined. The results are shown and discussed in /2/.

By use of eq (2) for frost resistance it is experimentally shown that the frost resistance on a critical depth from the wet surface of a material will be a function of time of water absorption of type:

$$ F = F_1 - k \cdot \log t $$

where $k$ is a constant, $t$ is time of water absorption, $F_1$ is the frost resistance at time one of the time unit chosen.

By determination of the constants $k$ and $F_1$ and by taking consideration to the rate of drying and the critical thickness eq (3) can be used for comparisons between frost resistance of different materials.

CONNECTIONS BETWEEN FROST RESISTANCE AND MATERIALS PROPERTIES (Reports 3 and 4)

The definition of frost resistance in eq (2) gives good possibilities of analyzing connections between materials structure and frost resistance. This problem can evidently be limited to an investigation of the influence of the relevant structural characteristics on $S_{\text{CR}}$ and on $S_{\text{ACT}}$.

The value of $S_{\text{ACT}}$ is mainly dependent on the pore structure. Connections between pore structure and water absorption is in turn treated by the "classical" moisture mechanics. Hence, very little is mentioned in the thesis about this part of the problem, /2, 3/.

In order to know about connections between materials structure and $S_{\text{CR}}$ it is necessary to know which freezing mechanism is predominant at freezing of different materials.

Freezing experiments have been performed where amount of ice formed, rate of ice formation and length change of specimen has been measured simultaneously during a freezing cycle, /3/. By such experiments it seems as if the major freezing mechanism, for both coarse-porous and fine-porous materials, is hydraulic pressure occurring when unfrozen water is expelled from the freezing site. In order to arrive to this conclusion certain considerations pertaining permeability of the materials at freezing temperature must be made. Coarse-porous materials have high permeabilities at ordinary temperatures but on the other hand they have small amounts of non-freezable water, /4/, which makes the permeability very much reduced at freezing temperatures. This explains why the same freezing mechanism can be valid for two so different materials as cement-paste and clay brick, /3/.

The hydraulic pressure theory predicts the existence of critical water-saturated volumes inside a material /3/. Such critical volumes (cri-
tical thicknesses of saturated slices) have been measured experimentally which also confirms the destruction by hydraulic pressure,\textsuperscript{3}.

The critical volume is, at fairly constant temperature conditions, only dependent on materials properties as strength, permeability, pore-size (influences the freezable water content,\textsuperscript{4}), specific heat (influences the rate of ice formation) etc. A property like strength or specific heat is in turn a function of more basic structural parameters like porosity and pore-size. Hence it is quite possible to evaluate connections between materials structure and critical distance,\textsuperscript{3}.

The existence of a critical degree of saturation is only a geometrical consequence of the existence of critical volumes.

The problem of finding a critical degree of saturation is therefore reduced to the problem of finding a geometrical connection between volume of air-filled pores, size of those pores and size of the water-filled critical volumes.

Such geometrical connections are found in literature. The final expression for $S_{CR}$ is\textsuperscript{1,3}.

$$S_{CR} = 1 - \frac{1}{(1 + \alpha f(V_{CR})) \cdot P(1 - K)}$$

where $\alpha$ is the mean specific surface of air-filled pores (inversely proportional to their size), $f(V_{CR})$ is a simple function of the critical water saturated volume, $P$ is total porosity and $K$ is non-freezable water as fraction of total porosity.

Consequently all parameters determining the value of $S_{CR}$ can be expressed in structural characteristics of the material. This has been done in\textsuperscript{3}.

**FREEZING CHARACTERISTICS OF PORE WATER (Report 4)**

The definition, eq (1), of degree of saturation demands that the freezable water content is known. Besides, a complete description of the connections between materials structure and frost resistance demands knowledge of the connections between pore structure and freezing characteristics of the pore-water, cf eq (4) where the freezable water is expressed implicitly in $V_{CR}$ and explicitly in $K$.

On basis of theoretical expressions for the freezing-point of a crystal in its own melt an expression is derived for the freezing point of pore-water as function of the pore-size,\textsuperscript{4}:

$$r = -\frac{2 \sigma_{LG} M}{\rho_L \Delta H} - \frac{1}{\Delta T} + 19.0 \times 10^{-10} \sqrt{\frac{1}{\Delta T}}$$

where $r$ is the pore radius in meters, $\sigma_{LG}$ is surface tension water-air, $\rho_L$ is the density of the water, $\Delta H$ is the molar heat of fusion, $T_0$ is the freezing point of bulk water and $\Delta T$ is the freezing point depression of pore-water. The second term is the thickness of the adsorbed layer on the pore-walls.
This equation has with good result been compared with semiempirical expressions found in literature.

Eq (5) gives possibilities of a calculation of pore-size distributions from determinations of non-freezable water contents. In /4/ is given the formulas for such calculations. This is a method of pore structure analysis that is completely unexploited as far as the author knew of, despite it gives many advantages.

The pore radius is also coupled to the pore-water pressure in a way which is normally expressed by Kelvin's law (or Laplace equation).

By combination of Kelvin's law and eq (5) it is possible to give a connection between freezing point depression, \( \Delta T \), and the relative humidity, \( \frac{p}{p_s} \), with which the material is in equilibrium;

\[
\Delta T = \frac{R \cdot T_0 (T - \Delta T)}{\Delta H} \ln \frac{p}{p_s}
\]

(6)

where \( R \) is the gas constant.

This equation has been used for comparison between experimentally determined non-freezable water contents at different temperatures and non-freezable water contents calculated from adsorption and desorption water-vapour isotherms for the same materials, /2/.

The non-freezable water contents are determined by melting experiments in adiabatic calorimeter. The calorimeter construction and results are accounted of in /2/.

Only comparisons with adsorption isotherms give satisfactory agreement, which confirms theoretical considerations that melting of ice is a process of adsorption.

Hence, on basis of experiments and theory, it has been proved that information on non-freezable water contents at different temperatures can be gained from the adsorption isotherm in the high pressure range (eq (6)) or from the pore-size distribution for pores with radii <1000 Å (eq (5)).

ACKNOWLEDGEMENTS

The author wants to thank professor Sven G Bergström, who initiated this research and who has provided many ideas. Another thank is transmitted to the Swedish Council for Building Research, which has financed the main part of the research. I also want to thank the whole staff at the Department of Building Materials at Lund Institute of Technology. Their help in the form of exchange of thoughts and practical work has been a main basis for this work. Finally, thanks Anne-Marie for your great support and encouragement!

LITERATURE

The most essential theoretical background to this work is the following reports;

R A Helmuth: Capillary size restriction on ice formation in hardened portland cement pastes.

T C Powers: The air-requirement of frost resistant concrete.