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Total Current Blockade in an Ultracold Dipolar Quantum Wire

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Cold-atom systems offer a great potential for the future design of new mesoscopic quantum systems with properties that are fundamentally different from semiconductor nanostructures. Here, we investigate the quantum-gas analogue of a quantum wire and find a new scenario for the quantum transport: Attractive interactions may lead to a complete suppression of current in the low-bias range, a total current blockade. We demonstrate this effect for the example of ultracold quantum gases with dipolar interactions.

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Introduction.—The electronic Coulomb blockade in mesoscopic quantum dots has been an intensive research topic the last two decades. The flow of electrons through a quantum dot between reservoirs is a versatile tool for addressing a wide range of fundamental effects, ranging from the structure of electronic many-particle states [1,2] and Kondo physics [3–5], to quantifying the spin dephasing due to coupling to nuclear degrees of freedom [6–8] or coherent effects [9].

Ultracold atoms in traps are very similar to quantum dots—a few quantum particles confined by a (often low-dimensional and harmonic) potential. What makes these systems particularly interesting is that one essentially can freely engineer their properties, and even control the shape and strength of the interparticle interactions. More recently this sparked great interest in making (quantum-)logical devices with ultracold atoms and molecules analogous to those in electronics and spintronics [10–15].

“Interaction blockade” as the cold-atom analog of an electronic Coulomb blockade [16] was experimentally first seen in tunneling processes in optical lattices [17] and analyzed theoretically for one-dimensional triple-well systems [18]. Atom trapping with numbers down to single-atom precision was reported in a remarkable recent experiment by Serwane et al. [19], reaching the few-body limit with full control over confinement and interparticle interactions. The experimental realization of quantum transport of cold atoms through a small quantum few-body system that is brought in contact with two large atomic reservoirs, however, has up to now posed a great experimental challenge. A first experimental breakthrough was reported recently by Brantut et al. [15], demonstrating the possibility of engineering both a ballistic and a diffusive channel between two cold-atom reservoirs, opening up a host of new perspectives in mesoscopic quantum physics.

Inspired by this recent experimental progress, we study the quantum transport through wirelike confinement of a few ultracold fermions. In the framework of the experiment by Brantut et al. [15], such a structure could be realized by two optical barriers within the channel, created by focusing two blue-detuned laser beams perpendicularly onto the channel.

A particularly interesting aspect of studying transport with cold atoms or molecules is the tunability of the interactions between the particles—often being of contact type, and experimentally controlled by Feshbach resonances. Here, we choose to study fermions with electric dipolar interactions that can be controlled by an external field [20]. Changing the interactions from repulsive to attractive, we report the occurrence of total current blockade, where the attractive interaction hinders transport for finite biases independent of the gate potential. While the total current blockade would also occur with attractive contact interactions, dipolar interactions also make it possible to study localization effects due to the long-range nature of the force, in much analogy to electrons in quantum wires [21].

The setup of the system described above is sketched in Fig. 1. Similar to the experiment in Ref. [15], two fermionic reservoirs with controllable difference in chemical potential $\Delta \mu$ are connected by a quasi-one-dimensional trap. In this region, the potential energy of the particles can be varied by the parameter $\mu_{\text{gate}}$ in full analogy to electrons in gated semiconductor nanostructures. The electric dipole moment $p$ of the particles can be orientated along an external field by a tilt angle $\Theta$ with respect to the $z$ axis along the quasi-one-dimensional channel (see Fig. 1). One can thereby also minimize the dipolar component of the particle interactions in the leads and stabilize the dipolar gas against collapse in the left and right reservoirs, required to be two dimensional and appropriately oriented with respect to the external field.

Model.—The interaction between two dipoles with distance $r$ and angle $\theta_{rd}$ between the dipole orientation and particle separation is generally given by [22,23]

$$V_{dd} = \frac{d^2}{r^3}(1 - 3\cos^2\theta_{rd})|_{r>0} + \frac{4\pi}{3} C d^2 \delta^3(r).$$

The coupling strength is $d^2 = p^2/(4\pi\epsilon_0)$, where $p$ is the dipole moment strength, $\epsilon_0$ is the vacuum permittivity, and...
FIG. 1 (color online). Upper panel: Schematic figure of the system. Lower panel: Sketch of the setup in analogy to the case of mesoscopic conductors. Two reservoirs with a degenerate gas of ultracold spin-half dipolar particles are connected via a quasi-one-dimensional structure, a “wire” of length 2a. The difference in chemical potential between the reservoirs, \( \Delta \mu \), creates a particle current if the dipoles can be added and removed from the wire. Levels in the wire may be tuned by a gate potential, \( \mu_{\text{gate}} \). The interaction between the particles in the wire can be varied by the tilt angle of the dipoles, \( \Theta \), and allows us to observe significantly different current patterns.

\[ C = 1. \quad \text{(For magnetic dipoles, } d^2 = \mu_0 \mu^2 / (4\pi) \text{ is significantly smaller, where } \mu_0 \text{ is the vacuum permeability, } \mu \text{ the magnetic moment, and } C = -2. ) \]

Within the quantum wire, the dipoles are confined in x and y by a two-dimensional harmonic oscillator of characteristic length \( l_\perp \), rendering a quasi-one-dimensional system in the z direction for small \( l_\parallel \). Integrating over the lateral x and y degrees of freedom one arrives at an effective one-dimensional dipole-dipole interaction

\[ V_{dd}^{\text{eff}}(z_1, z_2) = U_{dd}(\Theta) f \left( \frac{|z_1 - z_2|}{l_\perp} \right) + \frac{2C d^2}{3l_\perp^2} \delta(z_1 - z_2) \]

with \( f(u) = -2u + \sqrt{2\pi}(1 + u^2)e^{u^2/2}\text{erfc}(u/\sqrt{2}) \) where erfc is the complementary error function [24]. The interaction coefficient

\[ U_{dd} = -d^2 [1 + 3 \cos(2\Theta)] / (8l_\perp^2) \]

can be either positive or negative depending on the dipole tilt angle \( \Theta \). If the dipoles are aligned in the z direction (\( \Theta = 0^\circ \)) they attract each other, \( U_{dd} < 0 \), while they repel one another, \( U_{dd} > 0 \), if they are orientated perpendicular to the z direction (\( \Theta = 90^\circ \)). For an intermediate angle (\( \Theta_{\text{crit}} \approx 54.7^\circ \)) this long-range part of the dipole interaction vanishes.

In the z direction the wire is modeled as a finite square well (see Fig. 1) of width 2a and barrier height \( V_0 \). Applying the single-particle basis of eigenstates for this potential well, the configuration interaction method (exact diagonalization) is used to find the lowest energy states of \( N = 1 \) to \( N = 6 \) dipoles in the quantum wire. Here the dipolar particles are assumed to be spin-half fermions. In the following we use \( d^2 = h^2a/m, l_\parallel = 0.14a, \) and \( V_0 = 300h^2/ma^2 \). (For RbK molecules with \( p = 0.57 \) D [25] this corresponds to \( a = 0.6 \mu \text{m} \) and an energy unit of \( h^2/ma^2 = k_B 10 \) nK.)

Transitions between states of different \( N \) occur due to particle exchange with the reservoirs, as described by rates \( \Gamma_{a\leftrightarrow b} \) evaluated by Fermi’s golden rule. The corresponding matrix elements between the many-particle states are evaluated following the work of Refs. [26,27]. Assuming that the occupations of the single-particle states in the particle reservoirs are given by Fermi-functions with \( k_B T = 0.02h^2/ma^2 \), this provides a Pauli master equation for the probabilities of the different many-particle states in the confinement region. For the stationary state we obtain the (particle) current \( \dot{N} \) between the reservoirs and the (differential) conductance \( G = d\dot{N}/d\Delta \mu \).

**Main results.**—First we neglect the contact term of the dipolar interaction, which can be eliminated by Feshbach resonances [28], and obtain the conductance diagrams displayed in Fig. 2. For repulsive interactions between the dipoles, see Figs. 2(a) and 2(b); they resemble those of a Coulomb blockade in electron transport through nanostructures. In the diamond-shaped regions of vanishing conductance, the particle number \( N \) in the wire is fixed, and the current is strongly suppressed. At the borders between the \( N \)- and \( (N + 1) \)-particle region, conductance is possible due to single-particle transitions. This scenario does not depend on the specific form of the (repulsive) interaction [16,17]. For attractive interactions, see Fig. 2(e); we find a total current blockade at low detuning \( \Delta \mu \) independent of the gate potential \( \mu_{\text{gate}} \).

The total current blockade is associated with the vanishing of the diamonds for odd \( N \). This can be understood by the twofold degeneracy of the single particle levels due to the particle spin: The first particle enters the system at the level energy, while the second particle experiences an additional interaction energy \( U \) between the spin-degenerate particles in a level. The single occupancy of the level, i.e., a state with odd \( N \), is stable if the reservoirs allow for adding the first particle, but due to \( U > 0 \) not the second. Thus, the blockade diamonds with an odd number of particles \( N \) and lines of finite conductance at the separation to the blockade diamonds with even \( N \) appear in Figs. 2(a) and 2(b). With decreasing interaction the width of all diamonds shrinks and the width of the odd-\( N \) diamonds vanishes at \( U = 0 \) as can be seen in Fig. 2(d). Now, for negative \( U \) the situation of a single fermion in a level is unstable as it attracts a particle with the opposite spin. This instability does not allow for configurations with odd \( N \) for low \( \Delta \mu \). Therefore, single-particle transitions between the reservoir and the wire are excluded, resulting in the absence of current flow in the region of total current blockade; see the magenta shaded area in Fig. 2(e). (The case of two-particle transitions is addressed below.)
For weak interactions, this can be quantified by a quasi-independent-particle model: The single-particle level energies of the quantum well are approximated by

\[ E_n = \mu_{n+1} = \mu_{\text{gate}} + (n+1)E_1 + \frac{\hbar}{2n+\delta}U, \]

where \( U = 3l_1 U_{dd}/a \) and \( \mu_{\text{gate}} \) is the gate potential relative to the bottom of the well. Here, \( n = N/2 \) and \( \delta = 0 \) for even \( N \) while \( n = (N - 1)/2 \) and \( \delta = 1 \) for odd \( N \). The lines of the diamonds are given by the crossing points of \( E_n \) with the chemical potential in the left or right reservoir, respectively. The corresponding dashed (yellow) lines shown in Figs. 2(c) and 2(e) agree well with the main conductance lines obtained from the full many-particle calculation. Thus, correlations do not play any essential role here.

In contrast, such an approach does not hold for stronger interaction strengths. Here the many-particle states show strong localization effects as shown in Fig. 3 for the two-particle states. For \( \Theta = 90^\circ \) and to a smaller extent for \( \Theta = 60^\circ \), one observes two peaks in the particle density (left panel), and the pair-correlation function (right panel) shows that the probability of finding the two particles within the same peak is strongly reduced. This is the scenario of Wigner localization as very recently studied theoretically for cold polar molecules in Ref. [29]. In full analogy to mesoscopic electron conduction [21], signatures of this localization can be clearly detected in the conductance plots Figs. 2(a) and 2(b) where several, almost degenerate, lines are observed on the top of the diamonds, resulting from spin excitations of the localized particles. (We note that this scenario of Wigner localization could not arise in transport processes with atomic species that only interact through a contact interaction potential.)

Improved interaction model.—For attractive interaction (\( \Theta = 54.2^\circ \)), the pair-correlation function is shifted to the right; see the right panel of Fig. 3; i.e., the probability to find both fermions on the same spot is enhanced for the ground state. In this case the contact interaction in Eq. (2)
becomes relevant. Taking this term into account provides some modifications of the scenario depicted in Fig. 2, while the main features remain. For the case of electric dipoles, the contact interaction is repulsive and compensates a part of the long-range attraction, so that smaller angles Θ are required to observe the vanishing of the diamonds with odd N. Furthermore, because the particle density increases with the number of particles N, the contact interaction becomes more relevant for higher N, and thus smaller angles are required for the vanishing of diamonds with higher N [30].

Pair-tunneling.—Single-particle transitions between the reservoir and the wire are excluded for sufficiently low values of temperature and bias Δμ when U < 0. Two-particle transitions may occur due to higher-order processes in the coupling between the reservoirs and the wire [31,32]: Normal cotunneling results in a weak background conductance for any bias. Pair-tunneling, neglecting the effects of temperature and lifetime broadening, is only allowed for |E_{n+2} - E_{2n}| < Δμ, where E_N is the ground state energy of the N-particle state and n is an integer. When present, pair-tunneling gives a more pronounced contribution than cotunneling [31]. Being of second order, these processes scale as Γ^2, where Γ is the single particle transition rate. Thus, for sufficiently weak couplings they can be neglected compared to sequential single-particle tunneling.

Figure 4 shows the differential conductance of a single spin-degenerate level with U < 0, calculated by the second order von Neumann formalism [26,33]. For weak contact coupling, Fig. 4(a) displays only a small conductance at low values of Δμ. This can be attributed to a weak pair-tunneling background and to the temperature broadening \( \sim 3k_B T \) of the direct tunneling peaks at \( \epsilon_d = -U/2 \pm (\Delta μ + U)/2 \) for \( \Delta μ > -U \), which correspond to the inner (red) lines in Fig. 4. This demonstrates that the total blockade of conductance is verified for \( \Gamma \ll k_B T \ll |U| \), as is the case in Fig. 2(e).

On the other hand, as Γ approaches U, pair-tunneling becomes energetically allowed. Hence, we observe the onset of conduction along the outer (blue) lines \( |E_2 - E_0| = Δμ \) in Fig. 4(b). (In our case \( E_2 = 2\epsilon_d + U \) and \( E_0 = 0 \).) Normal cotunneling can also be observed as a weak background present at all Δμ and \( \epsilon_d \). Thus, the total blockade of conductance does not persist at strong couplings between the wire and the reservoirs. For even higher couplings, our model fails and Kondo-like effects become important [34]. This shows that the energy barriers confining the wire cannot be arbitrarily weak for the observation of the total current blockade, as otherwise pair-tunneling masks the scenario.

Experimental challenges.—From the experimental point of view, measuring a weak atomic current in a mesoscopic transport process appears challenging. In the experimental studies of quantum transport through atom traps by Brantut et al. [15], the integrated current is measured by a sensitive detection of population differences in the reservoirs. This opens up a new field of mesoscopic physics research. Complementary experimental information on the atomic current could, for instance, be inferred from a time-of-flight absorption image that renders the momentum distribution of the transported atoms. As an alternative, a stimulated Raman adiabatic passage of the atoms could be induced by irradiating the transport region with two spatially displaced laser beams (see, e.g., Ref. [35]). An atom that propagates through this irradiated region would then necessarily transfer a photon from one of the laser beams to the other, while an atom that propagates in the opposite direction would revert this photon transfer. Carefully measuring the net photon transfer between the beams after a suitable evolution time would then give rise to the integrated atomic net current across the atom-photon interaction region. We remark that standard techniques to detect individual atoms using fluorescence imaging [36,37] or electron beams [38] would not work in this context as they do not distinguish between left-moving and right-moving atoms.

Conclusions.—We have shown that dipolar quantum gases allow for the observation of a total current blockade for small differences in chemical potentials between the reservoirs. In this context the often neglected contact interaction part of the dipole-dipole interaction turns out to repress the onset of total current blockade.

From the experimental side, studies of quantum transport with ultracold atoms and the many-body effects of an interaction blockade are still in their infancy. Here, we highlighted the prospects for the specific example of a few-body system with dipolar interactions between the confined atoms. We demonstrated the possibilities offered by the tunability of the dipole-dipole interaction in a quasi-one-dimensional geometry by an external field.

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[30] We have observed this for, e.g., $C_2 = \frac{1}{4} C_14$, where the $N = 1$ diamond has already vanished, while the $N = 3$ diamond is very small, and the $N = 5$ diamond is still well established. In this case the total current blockade due to the attractive interaction extends only over a part of the spectrum.