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Limitations in the use of unipolar charging for electrical mobility sizing instruments: A study of the Fast Mobility Particle Sizer

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Abstract

A comparison between three different types of particle sizing instruments (Fast Mobility Particle Sizer (FMPS), Electrical Low Pressure Impactor (ELPI) and Scanning Mobility Particle Sizer (SMPS)) and one Condensation Particle Counter was made to compare instrument response in terms of size distributions and number concentration. Spherical oil droplets in 39 different sizes, with Geometric Mean Diameter (GMD) ranging from 50 to 820 nm were used as test particles. Furthermore, a characterization of the FMPS unipolar charger behavior was made to analyze the measured size distributions and number concentrations. The results show that all three sizing-instruments agree well for particle sizes below 200 nm, both in terms of size and number concentration, but the FMPS deviates clearly when particle sizes exceed 200 nm. Above this, the FMPS underestimates the particle size throughout the remainder of the size range, with an apparent upper limit for GMD of 300 nm. It also estimates a higher particle number concentration as compared to the other instruments. Analysis of the 22 FMPS electrometer currents and calculation of average number of charges per particle show a diameter dependence of response of $d_p^{1.21}$ for the FMPS unipolar charger. The resulting calculated electrical mobility showed a minimum in mobility for spherical particles at 577 nm, which indicates an interfering range of particles above the measurement range, but below the cut-off of the inlet pre-separator (1 µm). The study concludes that particle distributions with a true GMD above 200 nm cannot be measured reliably with the FMPS.
1. Introduction

Measurement of airborne particle size and number concentration in the sub-micron size range is important for understanding the properties and mechanics of airborne particles within the atmosphere and its radiative forcing (Seinfeld and Pandis, 2006). In addition, reliable measurements of exposures to particles from a few nanometers to several micrometers in size are increasingly becoming important in order to assess, measure and manage the inhalation risk of airborne fine, ultrafine particles and manufactured nanomaterials which are increasingly documented to be of serious concern regarding our respiratory human health (Dockery et al., 1993; Donaldson et al., 2004; Oberdorster et al., 2005; Oberdorster and Utell, 2002).

For studies performed at workplaces aiming at measuring manufactured nanostructured particles, the Scanning Mobility Particle Sizer (SMPS, Wang and Flagan, 1990) is the most common instrument to be used for measurements of particle size distributions in the sub-micron range (Brouwer et al., 2009; Kuhlbusch et al., 2011). The potential downside of this technique is the relatively low time-resolution where a full scanning time takes from 16 seconds up to several minutes, depending on desired size resolution and instrument response time, which can cause erroneous measurements during transient concentrations (Asbach et al., 2014; Yao et al., 2006; Zimmerman et al., 2014). Other common instruments used for particle sizing in this range include the Fast Mobility Particle Sizer (FMPS, TSI Inc. Shoreview, MN, USA) and the Electrical Low Pressure Impactor (ELPI, Dekati Ltd., Finland), which both have the advantage of 1 second time resolution. However, it is imperative that the gain in time resolution should not come at a too high decrease in precision and accuracy in the determination of particle size and concentration.

Several studies have been carried out which compare these three instruments in different regards and during measurement of a large number of different aerosols. Asbach et al. (2009) compared three different commercial SMPS systems and one FMPS by measuring NaCl particles (Geometric mean diameter ~ 30 nm) and soot agglomerates (70-90 nm). They found that the FMPS consistently measured slightly lower...
Geometric Mean Diameters (GMD) than the SMPS systems. In terms of concentration, the FMPS measurement was comparable to the SMPS systems for NaCl, but significantly higher for soot particles, likely due to the complex morphology of soot. Jeong and Evans (2009) compared the FMPS with a SMPS for measurements of urban ambient and indoor particles, rural ambient particles and laboratory particles. They found a strong correlation between the two instruments in terms of total concentrations but poor agreement in the shape of the measured size distributions. All tested aerosols had a GMD below 100 nm.

Leskinen et al. (2012) compared SMPS, FMPS and ELPI along with additional instruments to aerosols relevant for occupational health measurements. They found that the SMPS, FMPS and ELPI produced similar results for 30 nm ammonium sulphate particles in terms of concentration and GMD, but for larger size TiO$_2$ agglomerates and powder dusts with more complex morphology, the FMPS reported higher concentrations and smaller GMDs than the SMPS. Kaminski et al. (2013) compared eight commercial SMPS systems with three FMPSs using NaCl, DEHS and soot particles of various sizes. They found very good agreement for small nanosized (~40 nm) NaCl particles while FMPSs underestimated the 250nm DEHS particles by 20-26 % as compared to the SMPS systems. For the soot particles, the FMPS underestimated the particle sizes even more, up to 40 %. The study concluded that the agreement between FMPS and SMPS is linked to the particle size and morphology. Hornsby and Pryor (2014) compared four SMPS systems and one FMPS for particles with GMDs between 10 and 100 nm. They found low deviation for the FMPSs from the GMD (±7.5 %) as measured by the SMPS systems. Awasthi et al. (2013) compared the Engine Exhaust Particle Size (EEPS 3090, TSI Inc. Shoreview, MN, USA), which uses the same measurement design as the FMPS, with a SMPS for silver agglomerates, and showed that the EEPS consistently measured smaller number median mobility diameters and overestimated the total number concentration up to 67%. They also concluded that for small monodisperse particles (<80 nm), the EEPS measured diameters close to that of the SMPS but with a polydisperse distribution. No studies containing FMPS size distributions with a GMD higher than 200-250 nm could be found within the available literature by the authors.
This study was initiated by the observation that measuring the particle size distributions from powder agitation using rotating drum methods has been shown to produce inconsistent results when comparing size distributions measured with FMPS and ELPI, where the FMPS consistently showed a mode with the GMD of 200 nm, which is not observable in the ELPI data (Levin et al., In prep.). These data showing a mode with a GMD of 200 nm are consistent with data from several other dustiness studies, where the FMPS has been used to measure dust particles (Burdett et al., 2013; Jensen et al., 2009; Levin et al., 2014; Schneider and Jensen, 2008).

Previously, efforts to establish correction algorithms for the FMPS have been presented by Jeong and Evans (2009) and Zimmerman et al. (2015). The first study proposed an adjustment of measured FMPS number concentration in channels below 93.1 nm through an empirical correction established by comparing FMPS size distributions with that of a SMPS. The second study extended this correction by proposing an adjustment of size bins starting at 80.6 nm and above which broadens the upper limit of the instrument to 857 nm to compensate for the underestimation of particle sizes. Furthermore, they normalized each size bin with the ratio in total concentration between the FMPS and a water-based Condensation Particle counter (CPC). There is, however, a need to further test if such a correction holds true for particles larger than 300 nm, which was the upper size range in Zimmerman et al. (2015). Since no information on the influence of particles with a GMD above the measurement range of the FMPS but below the pre-separator has been found by the authors, this possible error source needed to be addressed.

This study aims to investigate the apparent size-dependent deviations of FMPS when compared to other particle sizing instruments such as SMPS and ELPI. While a large amount of studies have compared the instruments for <200 nm particles, scarce data exist for particle size distributions with geometric mean diameters in the remainder of the claimed FMPS size range reaching up to 560 nm. Because the FMPS samples particles up to 1 μm in size by pre-selection through a PM$_{1.0}$ cyclone, we have also studied the effect of particle size distributions with GMDs above the FMPS size classification limit (560 nm) on the
FMPS response. Finally, attempts were made to characterize the FMPS unipolar charger and calculate the charging profile with regard to particle size to further understand the instrument response to various particle sizes and possible interfering size ranges.
2. Methods

2.1 Instrumentation

Three types of instruments designed for size measurements of particles in the sub-micron size range were included in the study. Additionally, a CPC was added as a reference instrument for comparisons of total number concentration.

*Fast Mobility Particle Sizer (FMPS 3091, TSI)*

The FMPS (TSI, 2006) is a recently developed instrument based on the Electrical Aerosol Spectrometer (EAS, Tammet et al., 2002). While the EAS consists of two parallel compartments for measuring particle mobility, one with diffusion charging and one with field charging, the FMPS only used the diffusion charger part which positively charges the particles. In the EAS setup information from the field charging part was used in the classification of particles larger than 300 nm due to the conversion from mobility to particle size in this region becoming ambiguous in the diffusion charging part (Tammet et al., 2002).

After charging, the particles are separated in an electric field according to their electrical mobility and detected by 22 electrometers positioned in a vertical column. The measured currents are then corrected for multiple charges and image charges and then inverted from the 22 measured currents into 32 size channels ranging from 5.6 to 560 nm in electric mobility equivalent diameter. The measured size and concentration are therefore both dependent on the charging efficiency. Since the output contains more size channels than actual measurements, some assumptions must be made in the data inversion algorithm – these are, however, not disclosed by the manufacturer. The FMPS measures particle size distributions with a 1 second time resolution. Intake sampling for the FMPS is done at 10 l/min through a PM$_{1.0}$ cyclone. Two identical FMPS systems were used within this study, hereafter denoted as FMPS 1 & 2.
**Electrical Low Pressure Impactor (ELPI+, Dekati)**

The ELPI (Järvinen et al., 2014; Keskinen et al., 1992) uses a unipolar diffusion charger to charge the aerosol as it enters the instrument. The particles are size-separated according to their aerodynamic equivalent diameter in a cascade impactor where the particles are detected through charge measurements as they impact onto the 13 impactor plates. The final stage consists of a back-up filter stage. The measured currents in the ELPI+ are then corrected for multiple charges, image charges and then converted into concentrations specific for each size fraction ranging from 6 nm to 10 µm in aerodynamic equivalent diameter. Since the 14 measured currents directly correspond to the 14 size channels, and only concentration data is extracted from this, the data inversion is simpler and carries less assumptions than in the case of the FMPS. Intake sampling for the ELPI is done at 10 l/min and it measured particle size distributions with one second time resolution.

**Scanning Mobility Particle Sizer (SMPS)**

The SMPS (Wang and Flagan, 1990) used in this study consisted of a $^{63}$Ni aerosol neutralizer, a Differential Mobility Analyser (DMA, Vienna type, 28 cm; Winklmayr et al., 1991) and a CPC (CPC 3010, TSI; Mertes et al., 1995). It was built and intercompared according to current technical standards for mobility size spectrometers as described by Wiedensohler et al. (2012). The sheath air was dried using silica gel. The SMPS measures the mobility equivalent size of the particles in the range of 10 to 1000 nm, which is within the operating range of the CPC. To increase size resolution, the measurement range only covered a limited range, e.g. 50 to 500 nm, were the actual size range was adjusted to match the particle size distributions being measured.

The SMPS was operated with two adjacent 90 second scans, one with increasing voltage and one with decreasing voltage. Data inversion was performed with a Labview (National
Instruments, Austin, TX, USA) program (Löndahl et al., 2006) which also controlled the DMA
and CPC. Particle charge correction was performed according to the bipolar charge
distribution from Wiedensohler (1988) and, in the interval -2 to 2 elementary charges, from
(1963). The inversion of the SMPS data included correction for CPC smearing (Collins et al.,
2002), CPC counting efficiency (Zhou, 2001) and deviations from the ideal DMA transfer
functions (Collins et al., 2004). The DMA was run with an aerosol flow of 1 l/min and a sheath
air flow of 10 l/min.

Condensation Particle Counter (CPC 3007, TSI)

The CPC 3007 (TSI, 2002) measures the total number concentration of particles larger than
10 nm in the concentration range up to \(10^5\, \text{cm}^{-3}\) (Hämeri et al., 2002) with a 1 second time
resolution. The CPC 3007 samples inlet air with a flow of 0.7 l/min and has a manufacture
stated concentration accuracy of \(\pm 20\%\).

Sizing instruments were validated prior to the experiments using Polystyrene Latex Spheres (PSL, 80 and
150 nm) to ensure correct sizing and concentration. However, as reported previously, the FMPS is unable to
properly measure the monodisperse distributions that the PSL should give rise to due to its data inversion
where the measured particles always will be spread out over a minimum of 5 channels (Awasthi et al.,
2013; Leskinen et al., 2012; TSI, 2011). The CPC 3010 and CPC 3007 were also compared in terms of
concentration to be within the manufacture-stated precision. More information regarding control of
calibration can be found in the supplementary material.

2.2 Particle Generation and Test Setup
Test particles for the comparative studies were created by first aerosolizing a solution of \( \text{NH}_4\text{NO}_3 \) and water with a constant output atomizer using pressurized air of 1.5-3 bar depending on desired conditions. This aerosol was then dried using a diffusion dryer with silica gel to form salt particles with diameters of 40-50 nm. The dried salt particles were then introduced to the Condensation Aerosol Generator (SLG 250, Topas) where Di-Ethyl-Hexyl-Sebacat (DEHS) was condensed upon them to create spherical droplets. The oil droplet size could be varied from 50 nm up to 3 \( \mu \text{m} \) by varying the number of seed particles, oil temperature and flow rate through the saturator.

The formed DEHS droplets were directly emitted into a 1.3 m\(^3\) stainless steel chamber (Figure 1). The chamber was ventilated with HEPA-filtered air at 1 h\(^{-1}\) and used as a buffer volume to ensure stable concentrations. A joint aluminum sampling tube (\( \phi = 140 \text{ mm} \)) with a constant airflow of 40 l/min was used to distribute the stainless steel sampling tubes, 10 mm diameter to the instruments. Theoretical concentration differences along the sampling tube due to diffusional and gravitational losses were estimated to be less than 1 \% for the size range of interest in this study, which were experimentally confirmed.

Figure 1

A total of 39 measurement runs were made with the desired particle GMD varying from 50 to 800 nm. The desired Geometric Standard Deviation (GSD) of the distribution was around 1.3 to minimize errors in FMPS inversion due to monodisperse aerosol. A measurement run constituted of 30 minutes of continuous measurement of a stable (±10 \% in concentration) aerosol. Before a measurement started, all instrument flows were controlled, zero-tests were conducted using HEPA-filters, and electrometers zeroed where it was necessary. After each measurement run was concluded, the chamber was flushed with HEPA-filtered air to lower the background concentration (<50 cm\(^{-3}\)) in preparation of the next run.
2.3 Unipolar Charging

In unipolar diffusion charging, the aerosol is introduced to a volume with a high concentration of gaseous ions of a specific charge which are captured by the particles through the high diffusion coefficient of the ions. Fuchs’ limited sphere theory (Fuchs, 1963) together with corrections by Hoppel and Frick (1986) describes the theory of this particle charging. After passing through the charger volume, an average charge per particle, $\bar{q}$, has been imposed onto the particles. The average charge depends on the particle diameter, $d_p$, the ion density within the charger volume, $N_i$, and the particle residence time within the charger volume, $t$. The latter two relate to charging conditions and are properties of the charger design; they are often described as the so-called $N_i t$-product. For a specific $N_i t$-product and within a specific particle size range, the average charge per particle can be related to the particle diameter through a power-law such as:

$$\bar{q} \propto d_p^x$$

Besides the three parameters described above, unipolar charging may be influenced by several other factors such as particle morphology, particle dielectric constant, gas pressure temperature as well as ion properties such as mass and mobility (Kulkarni et al., 2011).

2.4 Data analysis

The raw data from the SMPS was inverted with regard to multiple-charge correction and diffusion losses. ELPI data was density-corrected with the DEHS density of 912 kg/m$^3$ adjusted for contribution of seed particle to density. To increase the comparability between instruments, the mobility diameter measured by FMPS and SMPS was converted into aerodynamic diameter using the assumption of spherical shape and the known density of DEHS using:

$$d_{aero}^2 \cdot C_{c,aero} = d_{mob}^2 \cdot C_{c,mob} \rho_p \rho_0$$

(2)
where \( d \) denotes particle diameter and \( C \) the Cunningham slip correction factor with subscripts \( \text{mob} \) and \( \text{aero} \) for mobility and aerodynamic equivalent diameters, respectively, \( \rho_0 \) is the standard density (1000 kg/m\(^3\)) and \( \rho_p \) is the particle density (Hinds, 1999). All measurement data were corrected for diffusional and gravitational sampling losses in tubing and tubing bends (<5%).

For each measurement run, 30 minutes of stable conditions were selected and the data of the FMPS and ELPI were averaged down to the same resolution as the SMPS (180 seconds). Fitting of log-normal functions to these size distributions was done to parameterize them into GMD, GSD and modal number concentrations using an automated algorithm (Hussein et al., 2005). In all cases of fitting, single-modal fitting was selected as the preferable choice. Means and standard deviations of the modal diameter and modal concentrations were then calculated. Data from the CPC was calculated into a mean value with standard deviations for the entire 30 minute measurement run.

For further analysis of the FMPS, the raw current response from the 22 electrometers was studied. To remove the effect of concentration differences between different measurement runs, all electrometer currents, \( I \), were normalized with the total concentration as measured with CPC 3007, \( N_{\text{CPC}} \). Thus the average number of charges per particle, \( \bar{n} \), which is equal to the average charge per particle, \( \bar{q} \), divided by elementary charge, \( e \), was calculated as:

\[
\bar{n} = \sum_{i=1}^{22} \left( \frac{I_i}{N_{\text{CPC}}Q_{\text{FMPS}}e} \right) \tag{3}
\]

where \( Q_{\text{FMPS}} \) is the flow of the FMPS. By calculating this average number of charges of distributions with various GMD, an exponential fit was made to determine the exponent \( x \) as shown in Equation 1 and the number of charges can be extrapolated for a large range of particle sizes. Finally, the electrical mobility, \( Z \), dependency on particle size for the FMPS unipolar charger can be calculated through:
\[ Z = \frac{\bar{n} e c_c}{3 \pi \eta d_p} \]  \hspace{1cm} (4)

where \( \eta \) is the viscosity of air.
Results and Discussion

Figure 2 shows typical size distribution measurements within the sub-micron range as measured by FMPS, SMPS and ELPI during four separate measurement runs. Visually, it appears that there is good agreement between all instruments for the distributions at 90nm and 150 nm (2a and 2b, respectively). As the particle sizes increase to 350 nm (2c), the FMPS distribution appears to be situated at a lower size (200 nm) than that of the other instruments. This becomes even clearer as the particle sizes grow further to 500 nm (2d), here it obvious that the FMPS modal number concentration (at 200 nm) is higher than the other instruments. The apparent measured particles in the lowest stage of the ELPI with 10 nm mid-point value in Figure 2a, b, and d are due to the higher noise ratio of the filter stage of the ELPI.

Figure 2

Figure 3 presents the fitted GMDs with standard deviations from all 39 measurement runs for the four instruments. The comparison between SMPS and ELPI fitted GMDs falls close to the (1 to 1)-line against those of the SMPS ($R^2=0.98$), and no size-dependent shift in the comparison can be observed. The FMPS data appear to behave in two ways depending on the size range: Up to GMDs of ~200 nm, the data correlates well ($R^2=0.94$); however, above 200 nm, it is clear that both FMPSs underestimate the modal sizes as compared to both SMPS and ELPI. Thereafter, they continue to produce distributions with GMDs between 200 and 300nm, well up into ranges above the 560 nm size-classification limit of the instrument. In no occurrence, as the particle sizes grew, did the FMPSs show only the tail end of a distribution, but rather showed a full particle mode.

Figure 3

The ratio in number concentrations contained in the particle modes for FMPS and ELPI against SMPS as well as the concentration ratio between CPC 3007 and the SMPS is shown in figure 4. In general, the number concentrations were between $3 \cdot 10^4$ and $6 \cdot 10^4$ cm$^{-3}$. There is a good correlation between SMPS and CPC
(Ratio=1.03±0.04) and SMPS-ELPI (Ratio=0.98±0.14). For the SMPS-FMPS comparison, there is a similar scenario to that of the GMD comparison, where there is a good correlation up until 200 nm (Ratio=0.99±0.12). For GMDs larger than this, the FMPS number concentration starts to exceed that of the SMPS. The number concentration ratio peaks around 500 nm where the number concentration measured by the FMPS is twice than that of the SMPS. After the particle GMD reaches the FMPS upper size limit, the ratio decreases again; however, it remains above 1 until the GMD reaches 650 nm. At this point, the majority of the particle distribution should lie outside the FMPS range.

The correction algorithm suggested by Zimmerman et al. (2015) is based on particle measurements up to 300 nm. However, the fact that the GMD response in the FMPS is not continuously increasing with the GMD of the measured aerosol above this range, Figure 3, points towards an upper limit for such a correction of bin sizes. In addition, such an algorithm for correction would still misclassify results given by erroneous measurements of particles larger than the measured size range but smaller than the pre-separator cut-off. Furthermore, the size dependent concentration over-estimation in Figure 4 suggests that a correction of FMPS concentration by that of a CPC would give an incorrect result in cases where a polydisperse aerosol is measured.

Figure 4

The concentration-normalized electrometer response for 22 different particle sizes, as measured with SMPS, between 50 and 800 nm is shown in Figure 5. From the response curves, it is clear that the particle size separation is more size sensitive for smaller particles than larger particles with the same size increment. In fact, particle GMDs between 550 and 800s nm give almost identical response and GMDs around 400-450 nm give a very similar response. It is also noticeable that even-though the three last distributions have a true GMD outside the FMPS range, the response from the last electrometer is decreasing for all of them. This all shows that as the particle size increases, it becomes more challenging to differentiate their particle size through this method.
The exponential fit of average number of charges per particle gave an exponent for the relationship between size and charge of 1.21±0.02. It should be noted that there is an uncertainty in this value due to the polydisperse nature of the aerosols. In the ideal case the charger would be characterized with mono-disperse particles but due to the FMPS inversion being unable to cope with this (TSI, 2011), distribution GSD varied from 1.25-1.35, as measured by SMPS, during the measurements. No previous value on the FMPS charger has been reported in literature, and these calculated values lie within the range of other reported values for unipolar chargers which lie between 1.32 and 1.91 for direct corona charges (Ntziachristos et al., 2004; Park et al., 2007), for indirect corona chargers between 1.11 and 1.36 (Fierz et al., 2007; Jung and Kittelson, 2005; Liu and Pui, 1975) and for turbulent jet chargers between 1.13 and 1.17 (Fissan et al., 2007; Jung and Kittelson, 2005; Park et al., 2007).

Figure 5

This 1.21 exponent in the power law can now be used for further analysis of the FMPS response to investigate whether the incorrect measurements stem from misclassification of particle sizes. Figure 6 shows a corrected concentration ratio for the FMPS defined as:

$$\frac{N_{FMPS}}{N_{SMPS}} \cdot \left(\frac{GMD_{FMPS}}{GMD_{SMPS}}\right)^{1.21}$$

This charging corrected ratio is now constant (0.94±0.11) within the measurement range of the FMPS above which it starts to decline. This constant behavior clearly suggests that the particles are detected in the FMPS but misclassified, e.g. a 500 nm particle interpreted as a 200 nm particle will give an overestimation in concentration by a factor of approximately 3 due to it carrying the charge equivalent of a 500 nm particle.

Figure 6
Furthermore, the fact that such high concentrations are measured even at GMDs higher than the upper limit of the FMPS might be linked to the fact that the inlet cyclone of the FMPS has an aerodynamic cut-off diameter of 1 \( \mu \)m. This means that particles in the size-range of 560-1000 nm will still enter the instrument, become charged and pass along the electrometer column. The calculated, Equation 4, particle electrical mobility of spherical particles after being charged by the FMPS charger as a function of size is presented in Figure 7. It is clear that the size dependency flattens out due to the Cunningham slip factor becoming a weaker function as the particle size grows and the electrical mobility reaches a minimum at 577±54 nm. Above this point there is actually an increase in electrical mobility up to the inlet pre-separator D_{50} of 1000 nm, and above. This would effectively mean that differentiation of particles in this region based on electrical mobility analysis after unipolar charging is becoming impossible and that large particles may even be unintendedly detected by an electrometer stage aimed for particles of smaller size but similar electrical mobility. According to this extrapolation, a spherical 1 \( \mu \)m particle, which has a penetration of 0.5, would have the same electrical mobility and be similarly interpreted as a 360 nm particle. Its concentration response would, however, be higher due to it carrying a higher charge. Also, it should be noted that as the function for average charge per particle exceeds the measured size range, the calculated power-law may not be precise due to shifting conditions.

*Figure 7*

For non-spherical particles, Shin et al. (2010) showed that agglomerates are able to carry more charge after unipolar charging than a spherical particle of the same mobility size and that the size dependency is steeper than that for spherical particles. This would infer that the magnitude of incorrect particle sizing in the FMPS would increase since the electrical mobility, compared to that shown in Figure 7, would increase and that the curve minima would move to smaller sizes. This would result in an incorrect response, both in terms of interpreted size and concentration, since a wider span of particle sizes within the measurement range will have the same electrical mobility. Furthermore, the influence of particles larger than the intended
measurement range (>560 nm) but below the aerodynamic cut-off of the cyclone (1 µm) would have a higher risk of being detected in the instrument electrometers and interfere on the measurements. In the case of agglomerates, the particle effective density can often be below unit density which results in a shifted cyclone cut-off point to a larger equivalent mobility diameter, which extends the interfering range of large particles in the measurements. Therefore, post-measurement corrections of FMPS results are challenging and would need to take the particle shape into account and can therefore not be independent of the particle source. In the presence of particles with a diameter above the mobility minimum, such a correction would be impossible due to the measurement ambiguity.

A separate possible explanation for the occurrences of underestimated GMDs and overestimated concentrations is the data treatment in the FMPS where the signal from 22 electrometers is inverted to 32 size channels. Such data inversion includes some type of data-fitting, e.g. log-normal or polynomial. Such a fitting would be useful in many applications such as atmospheric measurements were the particles fall into well-known modes within the range of the instrument (Birmili, 1998; Mäkelä et al., 2000). Similarly combustion processes mainly produce particle modes within this range. In many other applications such as dustiness testing, occupational powder handling and other industrial processes the freshly emitted aerosol might not assume these otherwise common particle modes. Using lognormal fitting for these types of particle size distributions may result in forcing the particle GMD into the measurement range, while increasing the particle numbers as the actual current is registered from large particles.

Other instruments using unipolar diffusion charging, such as DISCmini (Fierz et al., 2011) and nanoTracer (Marra et al., 2009) are known to be using fitting of the data and therefore report upper and lower limits on the GMD that can be measured within the total measurement range. For the FMPS, however, there are no such GMD limits reported in literature. If such a fitting takes place in the instrument, an extremely
important parameter to output would be the goodness of fit to ensure that the actual distribution is not an artefact of fitting.
3. Conclusions

In this study, we compared the measured particle size distributions of two FMPSs with that of one ELPI and a SMPS for 39 distributions of spherical DEHS particle distributions in a controlled test environment. The focus was put on the differences in the number size distribution log normal fitted GMDs and the modal number concentrations as measured by the FMPSs compared to the other instruments.

The study showed that the ELPI and SMPS agreed well, both in terms of GMD \( R^2=0.98 \) and number concentration \( \text{Ratio}=0.98\pm0.14 \), within the entire measured size range (50 to 850 nm). SMPS and ELPI also agreed well with the CPC in terms of total number concentration. The FMPSs agreed well with the other instruments for distributions with a GMD lower than 200 nm \( R^2=0.94 \). However, for particle size distributions with a GMD higher than ~200 nm neither the particle size nor concentration can properly be measured using the FMPS. Furthermore, the size response of the FMPS was not continuously increasing with increasing true particle size, rendering a correction algorithm difficult.

Calculations on the measured electrometer currents showed an increasingly similar response as the particle size distribution GMD increased ending with sizes above 500 nm giving almost identical responses. Fitting of average number of charges per particle and power-law fit resulted in a diameter dependence of charge response as \( d_p^{1.21} \) for the FMPS unipolar charger. The calculated electrical mobility showed a minimum in mobility for spherical particles at 577 nm, above which the electrical mobility increases with particle size. This indicates that there is an interfering range of particles above the measurement range, but below the cut-off (1 \( \mu \)m) of the inlet pre-separator that will be erroneously detected.

Although further data might be needed for decisive conclusions, indications were given that measured distributions with a GMD above 200 nm cannot be deemed reliable as it may originate from a distribution of larger size being incorrectly measured, if not confirmed through other means of measurement, as it might be an artifact distribution. As many industrial processes, such as production, pouring and packaging.
of nano-structured powder, are known to produce GMDs exceeding this or agglomerated particles where 
the effect will be even more pronounced, a secondary instrument should always be used to confirm particle 
observations. Based on this we recommend that reported size distribution with a GMD of 200 nm or above 
be further investigated as it might be caused by erroneous measurement.
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TSI, 2006. Fast Mobility Particle Sizer Spectrometer; Operation and Service Manual, TSI Incorporated, Shoreview, MN, USA.


Figure 1. Schematic overview of measurement setup. Tube lengths are not to scale.

Figure 2a-d. Size distributions as measured by FMPS, SMPS and ELPI in the sub-micron size range (90, 150, 350 and 500 nm as measured by SMPS and ELPI).
Figure 3. Fitted GMDs from FMPSs and ELPI plotted against GMDs from SMPS.

Figure 4. Concentrations of FMPS, ELPI and CPC normalized with that of SMPS. Dashed line indicates the upper measurement limit of the FMPS.
Figure 5. Electrometer response distribution normalized by total concentration. GMD values as measured by SMPS.

Figure 6. Concentration ratio between FMPS and SMPS corrected with respective GMD and charging parameter.
Figure 7. Calculated electrical mobility as a function of particle size. Dark shaded area denotes 95% confidence bounds based on fitting, light shaded area the size range of the FMPS. Dashed line indicates penetration through FMPS inlet cyclone pre-separator.